Atrial arrhythmias are electrical disturbances in the heart that can range in severity from annoying to life-threatening. The process of understanding these malformed rhythms must begin with a thorough comprehension of the normal spread of activation in the human heart. Experimental techniques, including recordings with microelectrodes¹ and normal spread of activation in the human heart.Experimental rhythms must begin with a thorough comprehension of the single ² or multiple ³,⁴ extracellular electrodes, have yielded a Luo-Rudy I¹⁵ kinetics. Recent reports have also emerged of sheet in space and penetrating it with a series of holes; they used described a flat, isotropic ²D sheet with an Earm and Noble ¹³ membrane. Virag et al¹⁴ represented the atria by folding a 2D sheet in space and penetrating it with a series of holes; they used Luo-Rudy ¹⁵ kinetics. Recent reports have also emerged of modeled activity in a single 1D pectinate muscle attached to an underlying rectangular sheet.¹⁶,¹⁷

In this article, we present the first membrane-based model of 3D conduction in a realistic human atrial geometry. The model includes both the left and right atria, including representations of the major atrial bundles and a right-sided endocardial network of pectinate muscles. The membrane’s kinetics are governed by the Nygren et al¹⁸ formulation for the human atrial cell. Because a simulation of wavefront conduction in a model of the atria with this degree of complexity has not heretofore been undertaken, the goals of this study are (1) to perform a comprehensive validation by comparing simulated patterns of activation and location conduction velocities during normal sinus rhythm and left/right pacing with published experimental observations and data and (2) to investigate the role of the well-defined atrial bundles in establishing the global activation sequence. The model provides a unique view of atrial activation, particularly in regions that cannot be easily recorded in patients. Consequently, activation maps are displayed in a 3D representation, avoiding the distortion that can arise from projecting 3D data onto a 2D surface.¹⁹ Although the focus of this work is on normal activation, the model provides a framework in which to easily conduct computer-based investigations of macroscopic atrial conduction, both normal and abnormal.

UltraRapid Communication

A Computer Model of Normal Conduction in the Human Atria

David M. Harrild, Craig S. Henriquez

Abstract—Although considerable progress has been made in understanding the process of wavefront propagation and arrhythmogenesis in human atria, technical concerns and issues of patient safety have limited experimental investigations. The present work describes a finite volume–based computer model of human atrial activation and current flow to complement these studies. Unlike previous representations, the model is three-dimensional, incorporating both the left and right atria and the major muscle bundles of the atria, including the crista terminalis, pectinate muscles, limbus of the fossa ovalis, and Bachmann’s bundle. The bundles are represented as anisotropic structures with fiber directions aligned with the bundle axes. Conductivities are assigned to the model to give realistic local conduction velocities within the bundles and bulk tissue. Results from simulations demonstrate the role of the bundles in a normal sinus rhythm and also reveal the patterns of activation in the septum, where experimental mapping has been extremely challenging. To validate the model, the simulated normal activation sequence and conduction velocities at various locations are compared with experimental observations and data. The model is also used to investigate paced activation, and a mechanism of the relative lengthening of left versus right stimulation is presented. Owing to both the realistic geometry and the bundle structures, the model can be used for further analysis of the normal activation sequence and to examine abnormal conduction, including flutter. The full text of this article is available at http://www.circresaha.org.

(Circ. Res. 2000;87:e25-e36.)

Key Words: atrial computer model ▪ cardiac propagation ▪ atrial conduction ▪ finite volume method
Materials and Methods

Anatomy of the Atrial Mesh

We have constructed a boundary-conforming mesh of the human atria comprised entirely of hexahedral (e.g., 6-sided) elements. The original set of surfaces used to guide the creation of the mesh was purchased from Viewpoint Digital. These surfaces were compared with literature reports of normal human atrial dimensions, where they diverged from these, they were modified accordingly. The dimensions of components of the mesh are given in supplemental Tables 1 through 3 (available in an online data supplement at http://www.circresaha.org). From the modified surfaces, a block-structured (multiblock) hexahedral mesh was made using TrueGrid from XYZ Scientific Applications.

The assembled human atrial mesh is presented in the center panel of Figure 1, in a left anterior view (see supplemental animation, spinning_mesh.mpg; available in an online data supplement at http://www.circresaha.org). The mesh includes 248,264 elements and is comprised of 7 constituent parts, each of which appears in the periphery of Figure 1. The block structure of each part appears in Figure 1, at the beginning of the chain of arrows leading to the full mesh. Figure 2 shows the left anterior (a) and posterior (b) views of the surface-rendered complete mesh. A detailed view of the right atrial endocardial structure appears in Figure 3. Two interatrial connections, Bachmann’s bundle and a region at the fossa ovalis (Figures 4a and 4b), carry current between the right and left atria. A number of meshed regions are defined to be bundles. These regions are the crista terminalis; the right atrial pectinate muscle network; Bachmann’s bundle; the intercaval bundle; and the limbus of the fossa ovalis (Figures 4a and 4b). The number of elements used in each component part of the mesh is scalable. The mesh used for simulations had element sizes that ranged from 50 to 1650 μm, with a mean interelement distance of 550 μm; 95% of the step sizes are smaller than 1060 μm. Most of the largest elements were located in the left atrial appendage.

Current Flow

The mathematics of the monodomain model and finite volume method used to model the spatial spread of electric current has been described by us previously. The transmembrane flow is represented according to the human atrial cell formulation of Nygren et al. The cell diameter listed by them of 11 μm gives rise to a surface-to-volume ratio of 3636/cm in our model.

Assignment of Regional Conductivities

To minimize complexity, only 3 conductivities are assigned to the model. The values of conductivities were selected to obtain realistic conduction velocities of ~60 to 75 cm/s in the bulk tissue, 150 to 200 cm/s in the bundles, and 30 to 40 cm/s in slow regions.

Because the model of Nygren et al assumes a surface-to-volume ratio of 3636/cm and produces a propagating action potential with a
relatively slow upstroke rate of rise of 110 V/s, it was necessary to
assign a high conductivity of 12.02 mS/cm to the bulk tissues to
obtain realistic wavespeeds. To implement fast propagation in the
longitudinal direction of the bundles, the conductivity along the
bundle axes is increased to 90.70 mS/cm; the transverse component
was the same as the bulk value. Slow isotropic conduction is
assigned to 2 regions, illustrated in Figure 4c. The first, the isthmus
of the right atrial floor, is a region of known slow conduction. The isotropic assumption here is a known simplification of the
structural reality. The interatrial connection at the fossa ovalis is the
other slow region, a reflection of the discordant activation of the
right and left atrial septa. The conductivity in these regions is
3.63 mS/cm. From 1D analysis, the ratio of the conduction velocities
in the fast and slow tissue, relative to the bulk tissue, for the given
conductivities should be 2.75 and 0.55 (given by the square root of
the conductivities). Differences from these values at specific
locations in the atria arise as a consequence of the influence of
geometry on the global conduction patterns.

**Numerical Issues**

The application of the finite volume method to the block-structured
grid gives rise to a sparse, symmetric positive–definite matrix. The
Cuthill-McGee algorithm was applied to reduce the matrix band-
width. A table-lookup for some of the rate constants in the Nygren et
al18 model was used to accelerate the calculations. A first-order,
semi-implicit time integration scheme was used with a fixed time
step of 20 μs. The system of equations was solved iteratively using
the conjugate gradient method with a convergence tolerance of 10−6.
A simulation of 125 ms of activation required 115 minutes of CPU

---

**Figure 2.** Left anterior (a) and posterior (b) views of the complete atrial model. SVC indicates superior vena cava; IVC, inferior vena cava; RA, right atrium; LA, left atrium; LAA, left atrial appendage; R/LPV, right/left pulmonary veins; pects, pectinate muscle network; BB, Bachmann’s bundle; and CT, crista terminalis.

**Figure 3.** View of the right atrial endocardial structure. Highlighted structures include the pectinates (pects), crista terminalis (CT), fossa ovalis (FO), coronary sinus (CS), limbus of the fossa ovalis (LFO), superior/inferior vena cava (SVC/IVC), and intercaval bundle (IB).
time on 28 processors on an IBM SP (Power 3, 200 MHz) at the North Carolina Supercomputing Center (Research Triangle Park, NC).

Although a complete convergence study on the effect of the spatial step sizes on the solution for the whole mesh was not possible owing to computational limitations, an analysis of a section of the right atrial free wall showed that increasing the density of elements from 27,440 to 92,610 (150% as dense in each direction) had a negligible effect on the activation pattern and total activation time (see supplemental Figure 1; available in an online data supplement at http://www.circresaha.org).

Results

Simulation of the Normal Activation Sequence in Human Atria

A simulation was performed to analyze the global conduction pattern in the model resulting from assigning a higher conductivity in the bundles than in the bulk tissue to represent the faster local conduction velocity. Figure 5 shows a number of snapshots of the progression of the expanding wavefront (color version, supplemental Figure 2, and supplemental animation, normal_act.mpg; available in an online data supplement at http://www.circresaha.org). In each case, the tissue activated at or before the indicated time is solid; the surrounding inactive tissue is translucent. The color gradient, in each figure, runs from earliest to latest activation for that time step. The capital letters in subsequent text refer to the corresponding letters in the figure.

A stimulus of 2 ms in duration and of sufficient strength to cause the initiation of a propagating wavefront is applied to the sinoatrial (SA) node region and by 10 ms, the wave begins to spread outward. By 20 ms, the wave quickly spreads anterior to the superior vena cava as a consequence of the increased conductivity in the crista arch (A). The anisotropy of the crista in the posterior wall is obvious here; the wavefront becomes nearly triangular as the crista activation precedes, and draws forth, that of the surrounding wall (B). Importantly, also, the depolarizing wave has now begun to spread through the proximal portions of the first 3 pectinate muscles (C). By 30 ms, a large portion of the superior wall has become active, and the excitation begins to descend the septal surface. The wave in the crista has already almost reached the inferior border of the posterior atrium. Almost all of the pectinates are active to some degree; conduction from the middle of the superior few pectinates to the endocardial wall is evident (D). The impulse in the first pectinate is nearing its terminus on the tricuspid rim. Importantly, also, the depolarizing wave has now traversed the interatrial Bachmann’s bundle and has merged with the anterior septal portion of the left atrial wall (E). The first activation of the left atrial surface has occurred just before this snapshot, at 29.7 ms. In the left atrial wall, an elliptic wavefront begins to expand, a reflection of the anisotropy of this bundle.

By 40 ms, the wavefronts have all but encircled the os of the superior vena cava. A more substantial portion of the left atrial wall has become active. Fully half of the pectinates are depolarized throughout; the adjacent muscle at their termini is activated by the impulse traversing these structures just before it is reached by the wave in the free wall proper. Septally, the wave has just reached the second interatrial connection, at the fossa ovalis (F). Ten milliseconds later, the
tip of the right atrial appendage borders on complete activation (G). The impulse has coursed through the entire length of every pectinate. Rapid conduction through Bachmann’s bundle in the left atrium has brought the impulse to the mouth of its appendage and has activated a substantial portion of the left atrial superior wall (H). The interatrial connection at the fossa ovalis is largely active. The influence of the posterior crista is still evident in the spiky projection of the wavefront toward this structure’s end. The next frame (60 ms) shows the progression of the right atrial septal wave (I), as the annulus of the tricuspid valve becomes increasingly surrounded by active tissue. The floor of the right atrium (J) remains mostly inactive. In the left atrium, the connection at the fossa ovalis has depolarized the region surrounding it (first occurring at about 51.5 ms). The wavefront begins to creep along the medial wall of the appendage (K) and posteriorly in the superior left atrial wall.

By 70 ms, the wave has completely encircled the mouth of the left atrial appendage. The interatrial connection at the fossa ovalis now contributes substantially to left atrial septal activation, and the left atrial anterosuperior wall is completely depolarized. The floor of the right atrium (J) remains mostly inactive. In the left atrium, the connection at the fossa ovalis has depolarized the region surrounding it (first occurring at about 51.5 ms). The wavefront begins to creep along the posteriorly in the superior left atrial wall.

Figure 5. Progression of the normally conducting wavefront. The number in the upper left of each panel indicates the time after stimulation, in ms. For each image, the colors run from blue (minimum) to red (maximum). See the text for specific comments on numbers and letters in the figure.
in Figure 7. The velocity in the bulk tissue averages \( \approx 74 \) cm/s. Within the bundles, the velocities are considerably greater, ranging between 110 and 177 cm/s. The slowest conduction, 40 cm/s, is found in the floor of the right atrium. Note that these velocities do not correspond to those of planar wavefronts but rather reflect the complex pattern of activation, front shape, and, in some regions, collisions of fronts (eg, left atrial appendage) that result naturally from the global activation sequence.

The sequence of activation in the right atrial septum is highlighted in Figure 8a (color version, supplemental Figure 3; available in an online data supplement at http://www.circresaha.org). Excitation progresses broadly in 2 directions, curling posteriorly around the superior vena cava and superiorly within the arch of the crista. The 2 waves collide within the posterior septal wall and accelerate along the fast bundles of the fossa ovalis rim. Traveling inferiorly, the wave becomes quite planar and bends around the os of the coronary sinus, terminating within the slow right atrial isthmus. In the left atrium, the septal activation sequence (Figure 8b) follows as a direct consequence of the right atrial patterns. Breakthrough at Bachmann’s bundle conducts anteriorly in an elliptical fashion, a consequence of this structure’s anisotropy. Later, conduction through the fossa ovalis region contributes to inferoposterior activation in the septum.

**Activation Patterns From Pacing**

In Figure 9 (right), a stimulus is applied to the right atrial appendage (color version, supplemental Figure 4, and animation, paced_ra.mpg; available in an online data supplement at http://www.circresaha.org). The early progression of the wavefront is circular. It first reaches the crista by retrograde conduction through the fast pectinate bundles rather than via the slow free wall (1 in Figure 9f). The wavefront, upon reaching the crista, becomes elongated along the axis of this bundle. The time for activation of all the right atrial tissue is \( \approx 116 \) ms; the last tissue activated is in its floor. The left atrium first becomes active at 44 ms via Bachmann’s bundle. The fossa interatrial impulse reaches the left atrium at 74.3 ms. Unlike the right atrial activation pattern, that of the left atrium is essentially normal. The activation of the last left atrial tissue occurs at 127.7 ms and is located at 2 in its posterior inferior region, slightly more lateral than in the normal case.

The conduction pattern resulting from pacing the left atrial appendage is shown in Figure 9 (left) (supplemental animation, paced_la.mpg; available in an online data supplement at http://www.circresaha.org). Leaving the appendage, the wavefront accelerates along the fast Bachmann’s bundle in the anterosuperior left atrial wall (3). It proceeds broadly along 3 routes in the left atrium. It courses into the superior wall, delineated by the ora of the pulmonary veins, and anterior to posterior on both sides of the mitral valve orifice. These wavefronts collide first in the posterior lateral wall (4) and, ultimately, in the inferior posterior medial region (5, at 123.0 ms).

The wave first gains entrance to the right atrium at 62.7 ms via Bachmann’s bundle. The right atrial fossa ovalis is activated simultaneously by a septal wave progressing inferiorly from Bachmann’s bundle and by the left atrial wave traveling across the interatrial connection there. These waves converge at \( \approx 99 \) ms. At the same time, the wave crests over the superiormost region of the right atrial wall, arriving at the SA node area and crista terminalis at about the same time that it reaches the annulus of the tricuspid valve. An interesting conduction pattern results in the superior pectinates, as waves conduct...
from both of the pectinate ends toward their centers. This configuration is shown at point 6 in Figure 9e, a snapshot of activity taken at 150 ms. The region of last activation remains in the atrial floor, occurring at \( \approx 169 \) ms; the total time for activation of the right atrium is thus \( \approx 106 \) ms.

**Discussion**

It has been asserted that the specifics of atrial anatomy are critically important in determining the spread of the activating wavefront.\(^6,40\) There are a number of well-defined uninsulated bundles in the atrial muscle within which current flow is rapid.\(^40,41\) These bundles include the crista terminalis, the pectinate muscles, Bachmann’s bundle, and the limbus of the fossa ovalis.\(^42\) As a consequence, these anatomical features were meshed as discrete structures in our model, and within these bundles, the hexahedral elements are aligned with their longitudinal axes. Their fiber angles could thus be aligned with the bundle axes, critical for the incorporation of anisotropy into the model. Anisotropy is an established and important property of the atrial bundles.\(^43\)
The bulk and bundle conductivities were set to produce local conduction velocities that were reasonable compared with experimental reports. With the assignment of only 3 conductivities, the global activation pattern could be analyzed. In subsequent text, comments are made regarding both the local conduction velocities and the global patterns of activation, and comparisons are made to experimental reports where such data are available.

Upon leaving the SA node, one pathway for the excitation wavefront in the model is along the crista terminalis in the posterior right atrial wall. Located at the intersection of the primitive atrium and sinus venosus, there is universal agreement that this prominent muscle bundle serves as a preferential pathway for atrial conduction.4,27,44,45 Boineau et al46 have presented mapping data from normal sinus in humans. The influence of the crista is visible in their data as a deflection in the isolines in the posterior right atrium and in the simulation in Figure 5 (especially panels a through c). The deflection is equally as obvious in maps of human right atrial activation published by Durrer et al.4 Measures of the conduction velocity in this structure (all from canine studies, perhaps owing to the difficulty of making this measurement in humans) have varied widely. A reasonable average, however, is 70 to 130 cm/s.44 The values in the model, between \( \approx 110 \) cm/s and 134 cm/s, fall within this range. It is interesting to note that the distal value of conduction velocity is notably smaller than the proximal one. A possible explanation for this slowing of the wavefront is that, as the wave advances, it becomes progressively more curved in nature and must excite a greater amount of surrounding tissue.47

An alternative exit from the SA node is into the surrounding free wall.46 This region, thin compared with the more substantial bundles characteristic of the right atrium,16 is assigned an isotropic conductivity in the model. An excitation wavefront nearly that is devoid of local deviation results. This pattern compares favorably with the Durrer et al data and the

---

**Figure 9.** Conduction pattern resulting from the application of a pacing stimulus to the right and left atrial appendages (right and left panels of the figure, respectively). a through d, Views of the overall activation maps (anterosuperior [a and b]; posteroinferior [c and d]). e and f, Snapshot of the tissue activated by 150 and 42 ms, respectively.
isolines in maps published by Boineau et al\textsuperscript{46} in which no preferential routes are evident within the free wall (except as noted below). A typical value for the simulated conduction velocity in the free wall is 74.6 cm/s. This number is within the range of 68 to 103 cm/s recently reported by Hansson et al.\textsuperscript{48}

Moreover, in that study, these researchers observed no directional difference in mean conduction velocity, supporting the isotropic assumption in the free wall of our model. Similarly, Gray et al\textsuperscript{46} reported an anisotropic ratio of nearly 1.0 in the sheep epicardial free wall, except at high pacing rates. The simulated free wall conduction velocity was subject to local variations. At a point of junction between an underlying pectinate muscle and the epicardial layer, for instance, it increased to a value of 95.4 cm/s. These variations have been reported in canine free wall measurements, where Wu et al\textsuperscript{17} have attributed such nonuniformities to the presence of gross endocardial structures such as pectinates.

Reported times for total activation of the right atrial free wall vary. Canavan et al\textsuperscript{59} indicate a duration of just $>80$ ms. Other studies, however, assert a time between 70 and 80 ms\textsuperscript{40} or $\approx 60$ ms.\textsuperscript{46} The corresponding value for our model is $\approx 60$ ms.

The conduction of the atrial impulse from the crista terminalis to the pectinate muscles is hidden from the epicardial views in published maps of human activation.\textsuperscript{46} In the model, the conduction velocities in the free-running portion of the pectinates are $\approx 160$ cm/s. Waves may also travel transversely between the pectinates at, for example, $\approx 116$ cm/s. Compare these speeds with the canine pectinate velocities of between 117 and 154 cm/s reported by Hayashi et al.\textsuperscript{42} The numbers cited by Spach et al in adult humans, between 58 to 78 cm/s for longitudinal conduction, are considerably lower. These velocities, however, were recorded subsequent to point stimulation. The resulting curved wavefront would be expected to propagate more slowly than the essentially planar waves existing in the pectinates during a normal sinus rhythm.\textsuperscript{47} It is worthy to note, in the model, the typically faster conduction velocities in the pectinate muscles compared with the crista terminalis, in spite of the assignment of the same longitudinal conductivities within these structures. The source of this disparity is found in the different environments of the 2 bundles; whereas the pectinates are largely free-running, the crista velocity is slowed by the surrounding electrically coupled tissue.

The modeled pectinate muscles are mostly discontinuous\textsuperscript{50}; the underlying endocardial surface is coupled to them at only one place during their length and at their ends. This anatomy, similar to that reported by Schuessler et al,\textsuperscript{50} gives rise to a difference in epicardial-endocardial conduction time (in particular, see Figure 6b) as the fast conduction in the pectinates precedes that of the overlying wall. This phenomenon of discordant epicardial-to-endocardial activation is the major result of the Schuessler et al study. In the model, the fast activation of the pectinates causes a region of breakthrough near the tip of the right atrial appendage. Jalife and Gray\textsuperscript{51} comment on a similar breakthrough pattern in the appendage in their studies with sheep.

The last pathway out of the SA node is via the arch of the crista, a structure in which modeled conduction proceeds at $\approx 122$ cm/s. This route brings the wavefront to the interatrial septum. Alternatively, the wavefront can reach this region by traveling down the crista and across the intercaval bundle or through the adjacent venous tissue (in the newborn, at least!). Experimental reports of activation in the right atrial septum have shown diverse patterns in mapped human patients. In one study in humans,\textsuperscript{52} the authors comment on the rapid spread of activation in the thick bundles of the septum, especially the anterior limbus of the oval fossa. These results are in agreement with an earlier report by Spach et al\textsuperscript{1} performed in dogs and rabbits. In that study, the authors assert that the patterns of septal conduction are, in large part, a simple consequence of the anatomy of the bundles contained therein.\textsuperscript{1} These observations are manifest, as well, in our modeled septal activation. The excitation impulse arrives at the septum as 2 waves. Within it, the wavefront is deformed when it reaches the fossa ovalis rim, where it travels at $\approx 115$ cm/s. In other regions in the septum, far from wavefront collision, the wave velocity averages $\approx 76$ cm/s. These velocities may be compared with a mean value of right atrial septal conduction velocity of 98 cm/s measured during electrophysiological study in 21 normal patients.\textsuperscript{54} Canavan et al\textsuperscript{59} report that the wavefront reaches the inferior atrial septum below the coronary sinus 85 ms after beat initiation. In the model, the point just distal to the coronary sinus in the direction of wave propagation is activated at 88 ms.

The crista terminalis, at its end, ramifies the floor of the right atrium. Within this region is located the so-called “isthmus” of slow conduction.\textsuperscript{26,53,54} Commonly considered to be bounded by the tricuspid annulus, the os of the coronary sinus, and the inferior vena cava. Modeled conduction is slow in this isthmus, declining to a velocity of $\approx 40$ cm/s. Experimental reports of this measure are quite variable. In 17 patients with symptomatic typical atrial flutter, the mean conduction velocities in the isthmus were 60 cm/s, which was slower than the velocities measured in other limbs of the flutter circuit ($\approx 100$ cm/s).\textsuperscript{55} A later study reports velocities of 83 to 89 cm/s in healthy patients but only 39 to 46 cm/s in patients predisposed to flutter.\textsuperscript{56} The authors conclude that the slow isthmus conduction is an important contributor to isthmus-dependent atrial flutter. In 1997, Feld et al\textsuperscript{56} reported similar numbers (50 to 55 cm/s in patients without flutter, 37 to 42 cm/s in patients with flutter). The conduction velocities in the modeled isthmus are consistent with those healthy patients at greater risk for flutter; when the bulk conductivity value was assigned to this region, however, the time for total right atrial activation decreased from 99.3 to 81.2 ms.

One of the pathways for interatrial connection is via Bachmann’s bundle. The modeled interatrial conduction velocity within this structure is quite rapid, $\approx 177$ cm/s. At the junction with the left atrial wall, however, the speed slows considerably, to $\approx 50$ cm/s. This deceleration occurs as the impulse undergoes a dramatic shift in fiber direction and an increase in electrical load. It then accelerates back to a value of $\approx 117$ cm/s within the left atrial wall. That Bachmann’s bundle is a region of fast conduction is not in dispute.\textsuperscript{42,43,56} Hayashi et al\textsuperscript{42} measured the conduction velocity of Bachmann’s bundle in dogs at 166 cm/s. Dolber and Spach\textsuperscript{43} reported values for longitudinal conduction within the adult dog of 92 to 167 cm/s. In the model, Figure 6c shows the
elliptical spread of electrical activation due to rapid spread in Bachmann’s bundle. The work of Hayashi et al.42 contains an illustration of the activation sequence in which the isolines are similarly displaced.

Bachmann’s bundle represents one of the two interatrial connections implemented in the model. The other is located in the region of the fossa ovalis.57,58 Activation of the septa of the right and left atria has been described as discordant,37 perhaps a reflection of a layer of connective tissue contained therein.52 Schuessler et al.48 reported, in dogs, that the left atrial septum consistently activated 10 ms later than the right. In recognition of this reality, the fossa ovalis interatrial connection was assigned the slow conductivity value. The modeled wave takes \( \approx 12 \) ms to traverse this structure. Breakthrough on the left atrial septum occurs in the model in 2 places (Figure 8b), and wavefront progression is primarily superior to inferior. Both of these observations are also made by Sun et al.,57 in their simultaneous study of the canine right and left septa. Recently, a third interatrial connection has been suggested in the region of the coronary sinus.57,58 No attempt was made to include this connection in the model.

Within the left atrium, modeled conduction completely engulfs the appendage at \( \approx 88 \) ms. Ultimately, the region of last activation within the atria occurs in the lateral posterior region, at 108.2 ms. The activation pattern in the data of Boineau et al.46 is similar. There, the excitation wave reaches the appendage tip between 80 and 90 ms. Later, 2 waves converge in the posterior lateral region, colliding soon after 110 ms. This time of last activation is by all accounts converging. This contrasts with the simulated activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreteness, a proper treatment of activity at the cellular scale would require a model with some level of this discreet...
Harrild and Henriquez

A Computer Model of Atrial Conduction

11


A Computer Model of Normal Conduction in the Human Atria
David M. Harrild, Craig S. Henriquez;

Circ Res. 2000;87:e25-e36
doi: 10.1161/01.RES.87.7.e25

The online version of this article, along with updated information and services, is located on the World Wide Web at:
http://circres.ahajournals.org/content/87/7/e25

Data Supplement (unedited) at:
http://circres.ahajournals.org/content/suppl/2000/09/22/87.7.e25.DC1
http://circres.ahajournals.org/content/suppl/2000/09/22/87.7.e25.DC2

Permissions: Requests for permissions to reproduce figures, tables, or portions of articles originally published in Circulation Research can be obtained via RightsLink, a service of the Copyright Clearance Center, not the Editorial Office. Once the online version of the published article for which permission is being requested is located, click Request Permissions in the middle column of the Web page under Services. Further information about this process is available in the Permissions and Rights Question and Answer document.

Reprints: Information about reprints can be found online at:
http://www.lww.com/reprints

Subscriptions: Information about subscribing to Circulation Research is online at:
http://circres.ahajournals.org//subscriptions/
<table>
<thead>
<tr>
<th>RA Anatomical Feature</th>
<th>Mesh Values (cm)</th>
<th>Reference Values (cm)</th>
<th>Reference Citation</th>
</tr>
</thead>
<tbody>
<tr>
<td>Anterior – posterior extent</td>
<td>4.6</td>
<td>2.8-5.2 (mean 3.8)</td>
<td>Cohen, 1995</td>
</tr>
<tr>
<td>Septal – lateral extent</td>
<td>4.2</td>
<td>2.9-5.3 (mean 3.8)</td>
<td>Cohen, 1995</td>
</tr>
<tr>
<td>Inferior – superior extent</td>
<td>4.5</td>
<td>Long, short axis 4.2, 3.6</td>
<td>Bommer, 1979</td>
</tr>
<tr>
<td>Wall Thickness</td>
<td>0.21-0.29</td>
<td>0.2 (mean)</td>
<td>Sunderman, 1949</td>
</tr>
<tr>
<td></td>
<td></td>
<td>0.05-0.35</td>
<td>Coffey, 1981</td>
</tr>
<tr>
<td></td>
<td></td>
<td>0.80-1.2</td>
<td>Hiraoka, 1998</td>
</tr>
<tr>
<td>Coronary Sinus Diameter</td>
<td>0.82-0.93</td>
<td>0.95-1.1</td>
<td>Cabrera, 1998</td>
</tr>
<tr>
<td></td>
<td></td>
<td>0.40-1.0 (mean .66)</td>
<td>Cohen, 1995</td>
</tr>
<tr>
<td>Tricuspid Valve Diameter (outside)</td>
<td>2.5-3.2</td>
<td>2.0-4.0 (mean 2.9)</td>
<td>Cohen, 1995</td>
</tr>
<tr>
<td></td>
<td></td>
<td>3.2-3.7</td>
<td>Kitzman, 1998</td>
</tr>
<tr>
<td></td>
<td></td>
<td>3.2-4.0</td>
<td>Sunderman, 1949</td>
</tr>
<tr>
<td>Crista Terminalis thickness</td>
<td>0.3</td>
<td>0.7-1.6 (mean 1.1)</td>
<td>Cohen, 1995</td>
</tr>
<tr>
<td>SA Node</td>
<td>0.82x0.49</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Intercaval Bundle Width</td>
<td>0.28</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Length</td>
<td>3.2</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Isthmus</td>
<td>1.2-2.5</td>
<td>1.6-4.0</td>
<td>Cabrera, 1998</td>
</tr>
<tr>
<td>Width</td>
<td>2.7-2.9</td>
<td>2.0-4.3</td>
<td>Cabrera, 1998</td>
</tr>
</tbody>
</table>

Supplemental Table 1 (methods) Summary of the measurements of the right atrial mesh and reference values.
<table>
<thead>
<tr>
<th>LA Anatomical Feature</th>
<th>Mesh Values (cm)</th>
<th>Reference Values (cm)</th>
<th>Reference Citation</th>
</tr>
</thead>
<tbody>
<tr>
<td>Anterior – posterior extent</td>
<td>4.0</td>
<td>2.0-5.2 (mean 3.8)</td>
<td>Cohen, 1995</td>
</tr>
<tr>
<td>Septal – lateral extent</td>
<td>4.0</td>
<td>2.4-5.2 (mean 3.9)</td>
<td>Cohen, 1995</td>
</tr>
<tr>
<td>Inferior – superior extent</td>
<td>4.1</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Wall Thickness</td>
<td>0.30-0.55</td>
<td>0.2 (mean)</td>
<td>Sunderman, 1949</td>
</tr>
<tr>
<td></td>
<td></td>
<td>0.3-0.5</td>
<td>Wang, 1995</td>
</tr>
<tr>
<td></td>
<td></td>
<td>0.05-0.35</td>
<td>Coffey, 1981</td>
</tr>
<tr>
<td>Mitral Valve Diameter (outside)</td>
<td>2.2-2.7</td>
<td>2.0-3.8 (mean 2.9)</td>
<td>Cohen, 1995</td>
</tr>
<tr>
<td></td>
<td></td>
<td>2.6-3.2</td>
<td>Kitzman, 1998</td>
</tr>
<tr>
<td></td>
<td></td>
<td>2.5-3.3 (mean 3.2)</td>
<td>Sunderman, 1949</td>
</tr>
<tr>
<td>Pulmonary Vein Diameter (inside)</td>
<td>0.8-1.0</td>
<td>0.7-1.6 (mean 1.1)</td>
<td>Cohen, 1995</td>
</tr>
</tbody>
</table>

**Supplemental Table 2** (methods) Summary of the measurements of the left atrial mesh and reference values.
<table>
<thead>
<tr>
<th>Anatomical Feature</th>
<th>Mesh Values (cm)</th>
<th>Reference Values (cm)</th>
<th>Reference Citation</th>
</tr>
</thead>
<tbody>
<tr>
<td>Superior &amp; Inferior Vena Cavae SVC diameter (in)</td>
<td>1.7</td>
<td>0.8-2.0 (mean 1.5) avg 1.6 0.9-2.8 (mean 1.8)</td>
<td>Cohen, 1995 Callans, 1999 Moreno, 1984</td>
</tr>
<tr>
<td>IVC diameter (in)</td>
<td>1.7</td>
<td>0.9-2.8 (mean 1.8)</td>
<td></td>
</tr>
<tr>
<td>Pectinate Muscles</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Length</td>
<td>2.2-3.1</td>
<td>0.1-0.3</td>
<td>Wang, 1995</td>
</tr>
<tr>
<td>Diameter</td>
<td>0.2-0.3</td>
<td>(10)</td>
<td>Papez, 1920</td>
</tr>
<tr>
<td>Number</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>LA Appendage</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Base Diameter</td>
<td>0.7-1.3</td>
<td>1.5-4.2 (mean 2.8)</td>
<td>Cohen, 1995</td>
</tr>
<tr>
<td>Inside</td>
<td>0.9-1.9</td>
<td>1.0-2.8 (mean 1.6)</td>
<td>Cohen, 1995</td>
</tr>
<tr>
<td>Outside</td>
<td>3.2</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Length</td>
<td>0.7-2.2</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Diameter (mid)</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Fossa Ovalis</td>
<td>0.90x1.15</td>
<td></td>
<td></td>
</tr>
<tr>
<td>RA side</td>
<td>0.90x0.80</td>
<td></td>
<td></td>
</tr>
<tr>
<td>LA side</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Bachmann’s Bundle</td>
<td>0.34-0.43</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Diameter</td>
<td>1.5</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Length (interatrial)</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

**Supplemental Table 3** (methods) Summary of the measurements of various parts of the atrial mesh and reference values.
Supplemental Figure 1: Conduction patterns and times as the spatial stepsize is varied. A portion of the right atrial free wall with the anisotropic crista is used for the simulation. The stimulus is applied near the location of the SA node. The left side shows an epicardial view while the right side shows the endocardial view. Isolines are separated by 5 msec. Panel (a) (27,440 elements) is the baseline case with the same element sizes used in the simulations described in the paper. Panel (b) (92,610 elements) shows the activation pattern computed on a finer mesh. Note that the patterns and the total activation times (49.3 vs 49.4 msec) are nearly the same for both the baseline mesh and the fine mesh.
Supplemental Figure 2: Color version of Figure 5.
**Supplemental Figure 3:** Color version of Figure 8.
Supplemental Figure 4: Color version of Figure 9.
Captions for Supplemental Animations that Accompany this Manuscript:

1. ("spinning_mesh.mpg"): The hexahedral atrial mesh described in the manuscript. The complete model includes 248,264 elements. (Accompanies Figs. 1, 2.)

2. ("normal_act.mpg"): The sequence of normal activation in the atrial model. Solid tissue becomes active at or before the time indicated in the animation. (Accompanies Fig. 5.)

3. ("paced_ra.mpg"): The activation sequence following the delivery of a pacing stimulus to the right atrial appendage. (Accompanies Fig. 9.)

4. ("paced_la.mpg"): The activation sequence following the delivery of a pacing stimulus to the left atrial appendage. (Accompanies Fig. 9.)